Theory and Applications of Approximate Model-Based Shielding for Safe Reinforcement Learning

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- Overview of shielding for RL
- 2 Bounded Safety
- 3 Approximate Model-based Shielding (AMBS)
- 4 Experiments and Applications

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# Section 1

Preface

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# Shielding for Reinforcement Learning



Figure: Shielding for reinforcement learning framework [Alshiekh et al., 2018]

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- **1** The shield is represented as a **finite state reactive system** S.
- 2 To construct the shield we require a **safety automaton**  $\varphi^s$ , a safety game is solved such that S realises the safety specification  $\varphi$  encoded by  $\varphi^s$  (i.e.  $S \models \varphi$ ).

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Limitations

- 1 Knowledge of the safety relevant dynamics of the environment are required **a priori** to construct the safety automaton.
- 2 Solving the safety game can be computationally expensive without additional assumptions.

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# **Bounded Prescience Shielding**



Figure: Bounded Prescience Shielding (BPS) [Giacobbe et al., 2021]

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1 A high-fidelity **simulator** is used to verify the safety and shield policies up to some bounded **look-ahead** horizon.

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Limitations

- 1 Rolling out a simulator can be computationally expensive.
- 2 In most cases BPS **cannot** be used during training, and only during deployment for short horizons (H = 5).



Figure: Latent shielding [He et al., 2021]

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1 During training the learned **world model** is used to estimate the probability of a violation in the near future.

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Limitations

- 1 Injecting noise into the action **overestimates** the probability leading to overly conservative behaviour.
- Intrinsic punishment and shield introduction schedules are required to resolve this, but they can be tricky to tune.
- S Limited by how far the world model can be rolled out (i.e. **short horizons** H = 15).

1 Classical shielding for RL operates with quite **restrictive assumptions**: access to the safety-relevant dynamics of the MDP.

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- 2 Methods such as BPS still assume access to a black-box simulator of the environment.
- Other methods (e.g. latent shielding) have a relatively short look-ahead horizon (H=15).
- 4 Most shielding methods only evaluate on quite **simple grid-world** environments.

- We will introduce a safe exploration problem based on the satisfaction of bounded safety defined in probabilistic computation tree logic (PCTL).
- We propose approximate model-based shielding (AMBS), a safe exploration strategy and model-based RL algorithm that leverages world models, and improves latent shielding by using safety critics, a cost predictor and a learned backup policy.

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- 3 We provide PAC-style probabilistic bounds on the probability of accurately detecting a safety violation and develop a strong theoretical justification for the use of **world models**.
- We apply AMBS to a variety of visual input settings, such as classic Atari games and continuous control problems from the Safety Gym suite.

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# Section 2

# Preliminaries

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Visual RL setting are typically modelled as partially observable MDP (POMDP). For our purposes we also extend the POMDP tuple to include state-dependent labels.

#### Definition (POMDP with labels)

A POMDP with labels is a 9-tuple  $\mathcal{M} = (S, A, p, \iota_{init}, R, \Omega, O, AP, L)$  where, S is the set of states, A is the set of actions,  $p : S \times A \times S \rightarrow [0, 1]$  is the **transition function**,  $\iota_{init} : S \rightarrow [0, 1]$  is the **initial state distribution** such that  $\int_{s \in S} \iota_{init}(s) = 1$ ,  $R : S \times A \rightarrow \mathbb{R}$  is the **reward function**,  $\Omega$  is a set of observations,  $O : S \times A \times \Omega \rightarrow [0, 1]$ is the **observation function**, which defines the probability of an observation conditional on the previous state-action pair, AP is a set of **atomic propositions** which maps to the set of states by the 'expert' **labelling function**  $L : S \rightarrow 2^{AP}$ .

At each timestep *t* the agent receives an observation  $o_t \in \Omega$ , a reward  $r_t \in \mathbb{R}$  and a set of labels  $L(s_t) \in 2^{AP}$ .

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# POMDP with Labels (continued)



Figure: Visual representation of a POMDP with labels

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Image: A matched block of the second seco

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In addition we are given a **propositional safety-formula**  $\Psi$ , e.g.

 $\Psi = \neg \textbf{collision} \land (\textbf{red-light} \Rightarrow \textbf{stop})$ 

for  $AP = \{$ **collision**, **red-light**, **stop** $\}$ . A state *s* is called **safe** if it satisfies the safety-formula  $\Psi$ , denoted *s*  $\models \Psi$ , which is determined by applying the **satisfaction relation** (from propositional logic),

$$egin{array}{l} s \models a ext{ iff } a \in L(s) \ s \models 
eg \Psi ext{ iff } s 
eq \Psi \ s \models \Psi_1 \land \Psi_2 ext{ iff } s \models \Psi_1 ext{ and } s \models \Psi_2 \end{array}$$

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#### Goal

Find a policy  $\pi$  that maximises reward, that is  $\pi^* = \arg \max_{\pi} \mathbb{E}[\sum_{t=0}^{\infty} \gamma^t \cdot r_t]$ , while minimising the cumulative number of violations of the safety-formula  $\Psi$  during training and deployment.

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Consider some fixed (stochastic) policy  $\pi$  and POMDP  $\mathcal{M}$ . Together  $\pi$  and  $\mathcal{M}$  define a **transition system**  $\mathcal{T} : S \times S \rightarrow [0, 1]$ , where  $\int_{s' \in S} \mathcal{T}(s, s') = 1$ .

#### Definition (Bounded Safety)

A finite trace with length *n* of the transition system  $\mathcal{T}$ , is a sequence of states  $s_0 \rightarrow s_1 \rightarrow ... \rightarrow s_n$  denoted  $\tau$ , the *i*<sup>th</sup> state of  $\tau$  is given by  $\tau[i]$ . A trace  $\tau$  satisfies bounded safety if and only if all of its states satisfy the state formula  $\Psi$  that encodes our safety constraints.

$$\tau \models \Box^{\leq n} \Psi$$
 iff for all  $0 \leq i \leq n, \tau[i] \models \Psi$ 

where  $\Box$  is the common temporal operator 'always' (or 'globally') [Baier and Katoen, 2008] and *n* is some look-ahead horizon.

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We can formalise  $\Delta$ -**Bounded Safety** in PCTL.

# Definition ( $\Delta$ -Bounded Safety)

A state  $oldsymbol{s} \in oldsymbol{S}$  satisfies  $\Delta$ -bounded safety as follows,

 $s \models \mathbb{P}_{\geq 1-\Delta}(\Box^{\leq n}\Psi)$  iff  $\mu_s(\{\tau \mid \tau[0] = s, \text{ for all } 0 \leq i \leq n, \tau[i] \models \Psi\}) \in [1 - \Delta, 1]$  (1)

where  $\mu_s$  is a well-defined probability measure induced by the transition probabilities T, over the set of traces staring from s and with finite length n.

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# **Motivating Example**

Example: avoiding irrecoverable states [Thomas et al., 2021].



Figure: To detect the **unsafe state** (pool of acid) at the end of the conveyor belt the agent needs a sufficient look-ahead horizon. During exploration the first agent (**left**) may fail to detect the pool of acid at the end of the conveyor belt and unknowingly venture down an irrecoverable. The second agent (**right**) has a sufficient look-ahead horizon and can avoid the pool of acid during exploration.

# Section 3

# Approximate Model Based Shielding (AMBS)

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• By using [Hafner et al., 2023] we can learn an **approximate** transition system  $\hat{T} \approx T$  that captures the underlying dynamics of the POMDP.

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- By sampling traces τ ∈ T we can check Δ-bounded safety, i.e, s ⊨ P<sub>≥1-Δ</sub>(□<sup>≤H</sup>Ψ); the Δ parameter meaningfully trades-off safety and exploration.

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- By sampling traces τ ∈ T we can check Δ-bounded safety, i.e, s ⊨ ℙ<sub>≥1-Δ</sub>(□<sup>≤H</sup>Ψ); the Δ parameter meaningfully trades-off safety and exploration.
- During training and deployment we can **shield** the agent by overriding 'unsafe' actions when necessary.

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"DreamerV3 learns a world model from experiences and uses it to train an actor critic policy from imagined trajectories. The world model encodes sensory inputs into categorical representations and predicts future representations and rewards given actions." [Hafner et al., 2023]

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# Recurrent State Space Model (RSSM)



Figure: Recurrent State Space Model (RSSM) [Hafner et al., 2023]

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# Additional Components (Cost Function)

- Cost predictor  $\hat{c}_t \sim p_{\theta}(\cdot | h_t, \hat{z}_t)$ implemented as an MLP mapping the learnt latent space  $\hat{s}_t = (h_t, \hat{z}_t)$  to estimated costs  $\hat{c}_t$ .
- Targets for the cost predictor,

$$c_t = egin{cases} 0, & ext{if } s_t \models \Psi \ C, & ext{otherwise} \end{cases}$$
 (2)

where C > 0 is a hyperparameter.

• Trained with the usual log likelihood gradients.



Figure: RSSM with costs

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# Additional Components (Safety Critics & Backup Policy)

Safety Critics:

• Trained with a TD3-style algorithm [Fujimoto et al., 2018] to estimate the cost value function,

$$\mathcal{V}^{\mathcal{C}}(m{s}) = \mathbb{E}_{\pi^{\mathsf{task}}}\left[\sum_{t=0}^{\infty} \gamma^t \cdot m{c}_t \mid m{s}_0 = m{s}
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• Used to check  $\Delta$ -bounded safety with a longer horizon.

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• Used to check  $\Delta$ -bounded safety with a longer horizon.

Backup Policy:

• The task policy  $\pi^{\text{task}}$  is trained to maximise reward, the backup policy  $\pi^{\text{safe}}$  is used as a **default safe policy**, it can be constructed in advance, however in most cases it must be trained with RL (to minimise costs),

$$\min \mathbb{E}_{\pi^{\text{safe}}} \left[ \sum_{t=0}^{\infty} \gamma^t \cdot \boldsymbol{c}_t \right]$$

(4)

# The Shielding Procedure



Figure: Checking  $\Delta$ -bounded safety

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# **1** Initialise replay buffer $\mathcal{D}$ with M random episodes.

## 2 Repeat until convergence:

- **3** Sample a batch  $B \sim D$  and update the RSSM with representation learning.
- 4 Sample latent trajectories with  $\pi^{\text{task}}$  and train  $\pi^{\text{task}}$  with RL to maximise reward.
- **5** Using the same trajectories, train the safety critics with maximum likelihood to predict the expected discounted cost.
- **6** Sample latent trajectories with  $\pi^{\text{safe}}$  and train  $\pi^{\text{safe}}$  with RL to minimise cost.
- **7** For  $\dot{K}$  environment interactions:
  - 8 Samples *m* trajectories in the world model with  $\pi_{task}$  to check if  $s \models \mathbb{P}_{\geq 1-\Delta}(\Box^{\leq H}\Psi)$
  - 9 If  $\Pr_{\pi \text{task}} \left[ \Box^{\leq H} \Psi \right] < 1 \Delta$ , then sample an action  $a \sim \pi^{\text{safe}}$  play with the backup policy, else sample an action the task policy  $a \sim \pi^{\text{task}}$ .
  - **1** Play *a* in the environment and observe o', *r*, L(s), append the experience to  $\mathcal{D}$ .

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# Probabilistic Guarantees

Let  $\mu_{s\models\phi}$  denote the probability that  $s\models\phi$ , where  $\phi=\Box^{\leq H}\Psi$ , note that  $s \models \mathbb{P}_{>1-\Delta}(\Box^{\leq H}\Psi)$  ( $\Delta$ -bounded-safety) if and only if  $\mu_{s\models\phi} > 1 - \Delta$ .

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#### Theorem 1 (Fully observable case)

Let  $\epsilon > 0$ ,  $\delta > 0$ ,  $s \in S$  be given. With access to the **true** transition system  $\mathcal{T}$ , with probability  $1 - \delta$  we can obtain an  $\epsilon$ -approximate estimate of the measure  $\mu_{s\models\phi}$ , by sampling *m* traces  $\tau \sim \mathcal{T}$ , provided that,

$$m \geq rac{1}{2\epsilon^2} \log\left(rac{2}{\delta}
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ight)$$

This result gives us a **sample complexity bound**, that dictates how many traces we need to sample (from T) to check  $\Delta$ -bounded safety with **high probability** (i.e  $1 - \delta$ ).

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Suppose we only have access to an **approximate transition system**  $\hat{T}$ . We provide the following sample complexity bound.

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## Theorem 2

Let  $\epsilon > 0$ ,  $\delta > 0$  be given. Suppose that for all  $s \in S$ , the total variation (TV) distance between  $\mathcal{T}(s' \mid s)$  and  $\widehat{\mathcal{T}}(s' \mid s)$  is **upper bounded** by some  $\alpha \leq \epsilon/n$ . That is,

$$D_{\mathsf{TV}}\left(\mathcal{T}(\boldsymbol{s}' \mid \boldsymbol{s}), \widehat{\mathcal{T}}(\boldsymbol{s}' \mid \boldsymbol{s})\right) \le \alpha \; \forall \boldsymbol{s} \in \boldsymbol{S} \tag{6}$$

Then with probability  $1 - \delta$  we can obtain an  $\epsilon$ -approximate estimate of the measure  $\mu_{s\models\phi}$ , by sampling *m* traces  $\tau \sim \hat{T}$ , provided that,

$$m \geq \frac{2}{\epsilon^2} \log\left(\frac{2}{\delta}\right)$$

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# Probabilistic Guarantees (Tabular Case)

When does  $D_{\mathsf{TV}}\left(\mathcal{T}(\boldsymbol{s}'\mid \boldsymbol{s}), \widehat{\mathcal{T}}(\boldsymbol{s}'\mid \boldsymbol{s})\right) \leq lpha$  ?

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ight) \leq lpha$$
 ?

#### Theorem 3

Let  $\alpha > 0$ ,  $\delta > 0$ ,  $s \in S$  be given. With probability  $1 - \delta$  the total variation (TV) distance between  $\mathcal{T}(s' \mid s)$  and  $\widehat{\mathcal{T}}(s' \mid s)$  is **upper bounded** by  $\alpha$ , provided that all actions  $a \in A$ with non-negligable probability  $\eta \ge \alpha/(|A||S|)$  (under  $\pi$ ) have been picked from s at least m times, where

$$n \geq rac{|\mathcal{S}|^2}{lpha^2} \log\left(rac{2|\mathcal{A}||\mathcal{S}|}{\delta}
ight)$$

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#### Theorem 4

Let  $b_t$  be a latent representation (belief state) such that  $p(s_t | o_{t \le t}, a_{\le t}) = p(s_t | b_t)$ . Let the fixed policy  $\pi(\cdot | b_t)$  be a general probability distribution conditional on belief states  $b_t$ . Let f be a generic f-divergence measure (TV or similar). Then the following holds:

$$\mathsf{D}_{\mathsf{f}}(\mathcal{T}(\mathsf{s}' \mid \mathsf{b}), \widehat{\mathcal{T}}(\mathsf{s}' \mid \mathsf{b})) \leq \mathsf{D}_{\mathsf{f}}(\mathcal{T}(\mathsf{b}' \mid \mathsf{b}), \widehat{\mathcal{T}}(\mathsf{b}' \mid \mathsf{b}))$$

where  $\mathcal{T}$  and  $\hat{\mathcal{T}}$  are the 'true' and approximate transition system respectively, defined now over both states *s* and belief states *b*.

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where  $\mathcal{T}$  and  $\hat{\mathcal{T}}$  are the 'true' and approximate transition system respectively, defined now over both states *s* and belief states *b*.

This result motivates the use of **world models** since the RHS appears in the RSSM loss function.

# Section 4

# **Experiments**

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Environment	Safety formula $\Psi$
Assault	$ eg$ hit $\wedge$ $ eg$ overheat
DoubleDunk	$ eg$ out-of-bounds $\wedge$ $ eg$ shoot-bf-clear
Enduro	<b>⊣crash-car</b>
KungFuMaster	$ eg$ loose-life $\wedge$ $ eg$ energy-loss
Seaquest	$(surface \Rightarrow diver) \neg hit \land \neg out-of-oxygen$



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# Results [Goodall and Belardinelli, 2023]

#### DreamerV3 DreamerV3 (AMBS) DreamerV3 (LAG) ION Rainbow Best Score ↑ 14738 44467 19832 9959 9632 Assault # Violations . 18745 12638 16802 24019 24462 Best Score ↑ 24 24 24 24 DoubleDunk # Violations ↓ 877499 66248 359018 188363 2369 2367 2365 2375 2383 Best Score ↑ Enduro 167933 132147 174217 129012 108000 # Violations 1 Best Score ↑ 97000 117200 97200 51600 59500 KungFuMaster # Violations 1 427476 10936 567559 284909 612762 Best Score ↑ 1940 34150 1900 4860 145550 Seaguest # Violations 1 73641 40147 64679 53516 67101 DreamerV3 (AMBS) DreamerV3 DreamerV3 (LAG) ION Rainbow 70204 20003 20001 60020 15003 50030 15020 40000 30000 20036 20000 2024.0 5000 10004 10025 1.5 2.0 2.5 95 10 15 20 25 30 35 1.0 1.5 2.0 2.5 10 15 20 25 30 35 40 0.5 0.5 (d) Violations (Seaquest) 🤍 🗠 (a) Reward (Assault) (b) Violations (Assault) (C) Reward (Seaguest) < A Charles University, Prague 11th April, 2023 33/41 Alex Goodall, Francesco Belardinelli (ICL) Approximate Model-based Shielding

#### Table: Episode return and cumulative violations at the end of training.

Shielded:

#### Unshielded:

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## Safety Gym vehicles:



(a) Point

(b) Car

## Safety Gym tasks and constraints:



(a) Goal positions



(b) Hazardous areas



(c) Vases

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#### Table: Episode return and cumulative violations at the end of training.

		AMBS + PENL	DreamerV3 + LAG	DreamerV3
PointGoal1 (1M) PointGoal2 (1.5M) CarGoal1 (1M)	Episode Return ↑ # Violations ↓ Episode Return ↑ # Violations ↓ Episode Return ↑ # Violations ↓	$\begin{array}{c} 17.32 \pm 3.29 \\ \textbf{9354} \pm \textbf{3734} \\ 10.64 \pm 2.61 \\ \textbf{29720} \pm \textbf{3850} \\ 8.87 \pm 2.95 \\ \textbf{11423} \pm \textbf{1479} \end{array}$	$\begin{array}{c} 19.15 \pm 0.92 \\ 24996 \pm 6627 \\ 15.78 \pm 1.84 \\ 52157 \pm 6151 \\ 11.23 \pm 4.10 \\ 28639 \pm 4644 \end{array}$	$\begin{array}{ c c c c c c c c c c c c c c c c c c c$



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- In contrast to latent shielding [He et al., 2021] our algorithm requires minimal hyperparameter tuning and no schedules and obtains further look-ahead capabilities with safety critics.

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- **3** We also develop a rigorous set of theoretical results that underpin AMBS.

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- In contrast to latent shielding [He et al., 2021] our algorithm requires minimal hyperparameter tuning and no schedules and obtains further look-ahead capabilities with safety critics.
- **3** We also develop a rigorous set of theoretical results that underpin AMBS.
- Our empirical results demonstrate that agents can benefit from shielding (AMBS) in both discrete (Atari) and continuous (Safety Gym) safety-critical domains.

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**1** What are the challenges associated with more sophisticated safety properties, e.g. regular safety properties, LTL safety properties? (currently working on this)

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- Investigate different shielding procedures how can we best leverage the backup policy, maybe integrate it into the policy gradient of the task policy? Can we use **model predictive control** (MPC) or planning as the backup policy?
- 3 Can we incorporate uncertainty estimation, **Bayesian world models** [As et al., 2022], to improve the agent learning and develop an 'uncertainty aware' shielding approach?

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# The End

# Thank you for listening!

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